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Exercises and Complements for the Introduction to Physics I  
for Students  
of Biology, Pharmacy and Geoscience

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Sheet 4 / 12.10.2020

**Solutions**

**Exercise 16.**

The force can be calculated by using the cosine theorem:

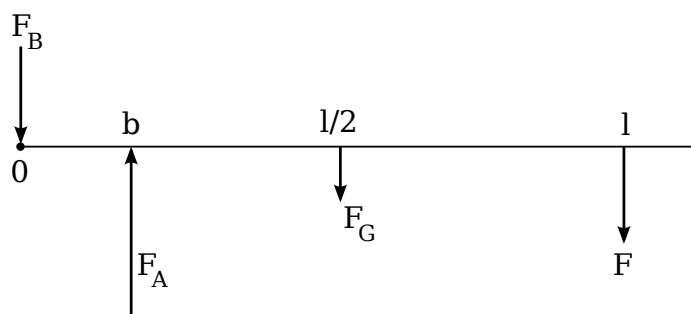
$$F_R = \sqrt{(4000 \text{ N})^2 + (7000 \text{ N})^2 + 2 \cdot 4000 \text{ N} \cdot 7000 \text{ N} \cdot \cos 120^\circ} = 6083 \text{ N}$$

**Exercise 17.**

1) No equilibrium ( $M_{tot} \neq 0$ ); 2) equilibrium ( $M_{tot} = 0$ ); 3) no equilibrium ( $F_{tot} \neq 0$ ); 4) no equilibrium ( $M_{tot} \neq 0$ ).

**Exercise 18.**

a)



b) The condition for a force equilibrium is :

$$F_A - F_B - Mg - mg = 0$$

The condition for a torque equilibrium acting on position B is:

$$F_A b - \frac{l}{2} Mg - mgl = 0$$

and from this  $F_A$  and  $F_B$  it can be calculated:

$$F_A = \frac{l}{b} \left( mg + \frac{1}{2}Mg \right) = 415.9 \text{ N}$$
$$F_B = F_A - (mg + Mg) = 286.4 \text{ N}$$

### Exercise 19.

On the object with the weight  $mg$  acting in the direction of the motion, the down-hill slope force  $F_H = mg \sin \alpha$  and in the opposite direction the friction force  $F_R = \mu F_N$  with the normal force  $F_N = mg \cos \alpha$ . If  $F_H$  is greater than  $F_R$ , then the object will slide downwards. The accelerating force is then:

$$F_H - F_R = mg(\sin \alpha - \mu \cos \alpha) = ma$$

resulting in the coefficient of sliding friction:

$$\mu = \frac{\sin \alpha - (a/g)}{\cos \alpha} = 0.20$$

In the limiting case where  $F_H = F_R$  (stiction), at  $\alpha = \beta_0$  (friction angle), is  $\mu_0 = \tan \beta_0 = 0.36$ .

### Exercise 20.

a) The kinetic friction on a horizontal plane is:

$$F = ma \quad \text{and} \quad F_R = \mu_g F_N = \mu_g mg$$

In the case where the system is in motion, the mass  $M$  which needs to be moved is composed of the two individual masses  $m_1$  and  $m_2$ :

$$M = m_1 + m_2$$

The effective acceleration is:

$$a = \frac{F - F_R}{M} = \frac{F}{M} - \mu_g g$$

b)  $F_1$ : only mass  $m_1$

$$F_1 = m_1 a + \mu_g m_1 g$$

$$F_1 = m_1 \left( \frac{F}{M} - \mu_g g \right) + \mu_g m_1 g$$

$$F_1 = \frac{m_1 F}{M}$$