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# Exercises and Complements for the Introduction to Physics I 

# for Students of Biology, Pharmacy and Geoscience 

## Exercise 31.

Since the two pistons are at the same height, the pressure of the liquid at both pistons (when the system is in equilibrium) is the same:

$$
p=\frac{F_{1}}{A_{1}}=\frac{F_{2}}{A_{2}}
$$

with

$$
F_{2}=\left(m+m_{K}\right) g \quad \text { follows } \quad F_{1}=\left(m+m_{K}\right) g \frac{A_{1}}{A_{2}}=87.2 \quad \mathrm{~N}
$$

## Exercise 32.

From the capillary law (script 107-9) it follows that:

$$
\sigma_{1,3}-\sigma_{1,2}=\sigma_{2,3} \cos \theta
$$

where $\sigma_{2,3}=\sigma$ is the surface tension of water towards air/vapor. Using this result and substituting it in the formula for calculating the height of the liquid column it follows:

$$
\begin{gathered}
r=\frac{2\left(\sigma_{1,3}-\sigma_{1,2}\right)}{h g \rho}=\frac{2 \sigma \cos \theta}{h g \rho}=1.13 \quad \mu \mathrm{~m} \\
d=2 r=2.26 \quad \mu \mathrm{~m}
\end{gathered}
$$

## Exercise 33.

(a) In general, according to Bernoulli:

$$
p_{1}+\rho g h_{1}+\frac{1}{2} \rho v_{1}^{2}=p_{3}+\rho g h_{3}+\frac{1}{2} \rho v_{3}^{2}=\text { const }
$$

For this exercise: $p_{1}=p_{3}=$ the pressure of air, $h_{1}=0, h_{3}=h_{r}+h_{w}, \rho$ density of water, and $v_{3}=0$ (velocity at point 3 , see figure) since the level of the water is constant.

$$
\frac{1}{2} \rho v_{1}^{2}=\rho g\left(h_{r}+h_{w}\right) \quad \Rightarrow \quad v_{1}=\sqrt{2 g\left(h_{r}+h_{w}\right)}=16.57 \mathrm{~m} / \mathrm{s}
$$

(b) Due to the equation of continuity, it follows:

$$
v_{2} A_{2}=v_{1} A_{1} \quad \text { with } \quad A_{i}=\pi\left(\frac{d_{i}}{2}\right)^{2}
$$

where $A_{i}$ is the cross section at the corresponding position. From this it follows:

$$
v_{2} d_{2}^{2}=v_{1} d_{1}^{2} \quad \Rightarrow \quad v_{2}=7.36 \mathrm{~m} / \mathrm{s}
$$

(c) Using again the Bernoulli equation:

$$
p_{2}+\rho g h_{2}+\frac{1}{2} \rho v_{2}^{2}=p_{3}+\rho g h_{3}+\frac{1}{2} \rho v_{3}^{2}=\text { const }
$$



Here: $p_{3}=p_{0}=$ pressure of air, $h_{2}=h_{r}, h_{3}=h_{r}+h_{w}, v_{2}$ calculated in (b), $v_{3}=0$.

$$
p_{2}=p_{0}+\rho g h_{w}-\frac{1}{2} \rho v_{2}^{2}=1.11 \quad \mathrm{bar}
$$

## Exercise 34.

(a) The flow of water through a cylindrical tube is described by:

$$
R_{0}=\frac{8}{\pi} \frac{\eta L}{r_{0}^{4}}
$$

The total resistance of the new tube is equal to the resistance of the four parallel tubes:

$$
\frac{1}{R_{n}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}+\frac{1}{R_{4}}=\frac{4}{R_{0}}
$$

Therefore is:

$$
\begin{aligned}
& R_{n}=\frac{1}{4} R_{0} \\
& \frac{8 \eta L}{\pi r_{n}^{4}} \stackrel{!}{=} \frac{1}{4} \frac{8}{\pi} \frac{\eta L}{r_{0}^{4}} \\
& \Rightarrow r_{n}=\sqrt[4]{4} r_{0}=\sqrt{2} r_{0}=0.141 \mathrm{~m}
\end{aligned}
$$

(b) Reynolds number:

$$
\begin{aligned}
I_{0} & =I_{1} \\
4 v_{0} A_{0} & \stackrel{!}{=} v_{1} A_{1} \\
\Rightarrow v_{0} & =\frac{1}{2} v_{1}
\end{aligned}
$$

Reynolds number: $R e=\frac{\rho v d}{\eta}$

$$
\begin{gathered}
\frac{R e_{0}}{R e_{1}}=\frac{v_{0} r_{0}}{v_{1} r_{1}} \\
\frac{R e_{0}}{R e_{1}}=\frac{v_{0} r_{0}}{2 v_{0} \sqrt{2} r_{0}} \\
\frac{R e_{0}}{R e_{1}}=\frac{1}{2 \sqrt{2}}
\end{gathered}
$$

(c) In the case of $A_{1}$ a turbulent flow is more probable. The velocity $v_{1}$ is higher and therefore the Reynolds number $R e_{1}$ is closer to the critical Reynolds number where turbulent flow occurs.

## Exercise 35.

(a) The forces can be described by the following equations:

$$
\begin{aligned}
m g & =V_{K} \rho_{K} g \\
F_{A} & =V_{W} \rho_{W} g
\end{aligned}
$$

where $V_{K}$ is the volume of the cuboid and $\rho_{K}$ the density, $V_{W}$ is the volume of the cuboid which is in the water and $\rho_{W}$ is the density of water. From this it follows:

$$
V_{K} \rho_{K}=V_{W} \rho_{W} \quad \Rightarrow \quad \frac{\rho_{K}}{\rho_{W}}=\frac{V_{W}}{V_{K}}=\frac{90}{100} \quad \Rightarrow \quad \rho_{K}=\frac{90}{100} \rho_{W}
$$

(b) Due to the additional buoyancy of the oil, the volume of the cuboid which enters the water is smaller.


