



Exercises and Complements for the Introduction to Physics II
for Students
of Biology, Pharmacy and Geoscience

Sheet 5 / 30.03.2022

Solutions

Exercise 17.

From the Lorentz force on a wire/conductor (**Script: 307-3**)

$$F_L = IlB$$

and the force of gravity

$$F_G = mg = \rho A l g$$

follows:

$$\tan \varphi = \frac{F_L}{F_G} = \frac{IB}{\rho A g} = \frac{jB}{\rho g} = 0.302 \quad \Rightarrow \quad \varphi = 16.8^\circ$$

where $j = I/A$ is the current density.

Exercise 18.

From the energy equation/balance it follows that the energy from the acceleration due to magnetic field = kinetic energy:

$$\begin{aligned} E_b &= E_{kin} \\ eU &= \frac{1}{2} m_1 v^2 \end{aligned}$$

follows:

$$v = \sqrt{\frac{2eU}{m_1}} = 8.755 \cdot 10^4 \frac{\text{m}}{\text{s}}$$

and thus, from the force balance in the circular path:

$$\begin{aligned} \text{Lorentz-force} &= \text{Centrifugal-force} \\ F_L &= F_Z \\ evB &= \frac{m_1 v^2}{r_1} \end{aligned}$$

(a) For the magnetic field, this results in:

$$B = \frac{\sqrt{2(m_1/e)U}}{r_1} = 0.18 \text{ T}$$

(b) The slightly heavier ^{65}Cu -ion describes a circular path with the radius:

$$r_2 = r_1 \sqrt{\frac{m_2}{m_1}} = 322.2 \text{ mm}$$

In the case of a semi-circular orbit, the detection points of the two types of ions are thus separated by the distance $\Delta x = 2(r_2 - r_1) \approx 10 \text{ mm}$.

Exercise 19.

(a) See Script 307-11.

$$B = \frac{\mu_0 N I}{l} \quad \Rightarrow \quad I = \frac{B_h l}{\mu_0 N} = 0.33 \text{ A}$$

(b) So that the field B_H from Earth can be compensated, the field B_S from the coil must point to the right. With the “right-Hand rule” one realizes the current must be I_+ .

Exercise 20.

As a result of the temporal change of the magnetic flux Φ inside the coil when switching it off, a short-circuit happens in the coil itself

$$I = \frac{U_{ind}}{R} = -\frac{N}{R} \frac{d\Phi}{dt} = -\frac{L}{R} \frac{dI}{dt}$$

inducing therefore the ohmic resistance of the winding $R = U_0/I_0$ and inductance of the coil $L = \mu_r \mu_0 N^2 A/l$, where $A = \pi d_E^2/4$ is the cross-section and $l = 2\pi r = \pi d_S$ the length. We apply the numerical values $R = 38 \Omega$ and $L = 67.9 \text{ mH}$. Writing in terms of I :

$$\frac{dI}{I} = -\frac{R}{L} dt$$

After integration, with initial condition $I(t=0) = I_0$:

$$\ln I - \ln I_0 = \ln \frac{I}{I_0} = -\frac{R}{L} t \quad \text{bzw.} \quad I(t) = I_0 \exp^{-(R/L)t}$$

For $t = 1 \cdot 10^{-3} \text{ s}$ follows $I(t = 1 \cdot 10^{-3}) = 2.0 \text{ A}$.